Ανισότητες για συμμετρικά πολυώνυμα και ροπές αθροίσματος εκθετικών τ.μ.

Σιλουανός Μπραζιτίκος 23 Μαΐου, 2025

Περίληψη

We establish L_2 -type inequalities for the complete homogeneous symmetric polynomial $h_d(a_1, \ldots, a_n)$, resolving a conjecture of Hunter and highlighting its probabilistic interpretation as the moment of a marginal of a standard exponential random vector. Our analysis is divided into three distinct regimes:

- (i) the conditional case, where the geometric constraint $\sum_{i=1}^{n} a_i = 0$ is imposed;
- (ii) the positive case, where all coefficients are positive; and
- (iii) the unconditional case, with no assumptions on the coefficients.